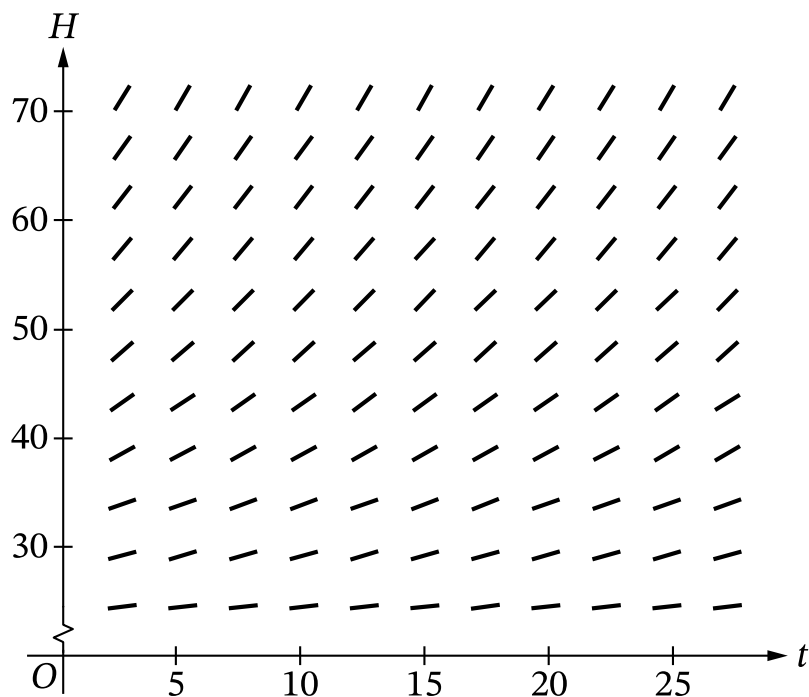


3. A pie is taken from a hot oven and put on a table. The internal temperature of the pie at time  $t$  minutes can be modeled by the function  $H$  that satisfies the differential equation  $\frac{dH}{dt} = -\frac{1}{15}(H - 20)$ , where  $H(t)$  is measured in degrees Celsius and  $H(0) = 75$ . For  $t > 0$ , it is known that  $20 < H(t) < 75$ .

### Part A

Explain why the following could not be a slope field for the differential equation

$$\frac{dH}{dt} = -\frac{1}{15}(H - 20).$$



### Part B

Find the slope of the line tangent to the graph of  $H$  at time  $t = 0$ . Show the work that leads to your answer.

### Part C

It can be shown that  $\frac{d^2H}{dt^2} = \frac{1}{225}(H - 20)$ . The line tangent to the graph of  $H$  at time  $t = 0$  is used to approximate  $H(5)$ , the internal temperature of the pie at time  $t = 5$ . Is this approximation an overestimate or an underestimate for the actual value of  $H(5)$ ? Give a reason for your answer.

### Part D

Use separation of variables to find an expression for  $H(t)$ , the particular solution to the given differential equation with initial condition  $H(0) = 75$ .