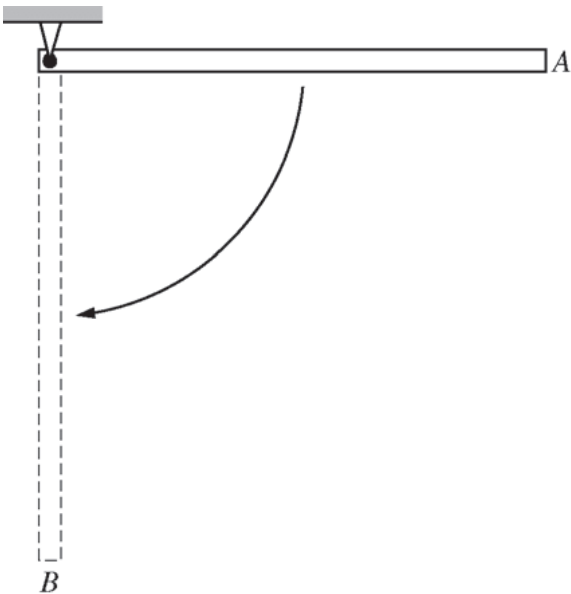


Mech.3.

A uniform, thin rod of length  $L$  and mass  $M$  is allowed to pivot about its end, as shown in the figure above.

- (a) Using integral calculus, derive the rotational inertia for the rod around its end to show that it is  $ML^2/3$ .



The rod is fixed at one end and allowed to fall from the horizontal position  $A$  through the vertical position  $B$ .

- (b) Derive an expression for the velocity of the free end of the rod at position  $B$ . Express your answer in terms of  $M$ ,  $L$ , and physical constants, as appropriate.

An experiment is designed to test the validity of the expression found in part (b). A student uses rods of various lengths that all have a uniform mass distribution. The student releases each of the rods from the horizontal position  $A$  and uses photogates to measure the velocity of the free end at position  $B$ . The data are recorded below.

|                |      |      |      |      |      |      |
|----------------|------|------|------|------|------|------|
| Length (m)     | 0.25 | 0.50 | 0.75 | 1.00 | 1.25 | 1.50 |
| Velocity (m/s) | 2.7  | 3.8  | 4.6  | 5.2  | 5.8  | 6.3  |
|                |      |      |      |      |      |      |
|                |      |      |      |      |      |      |

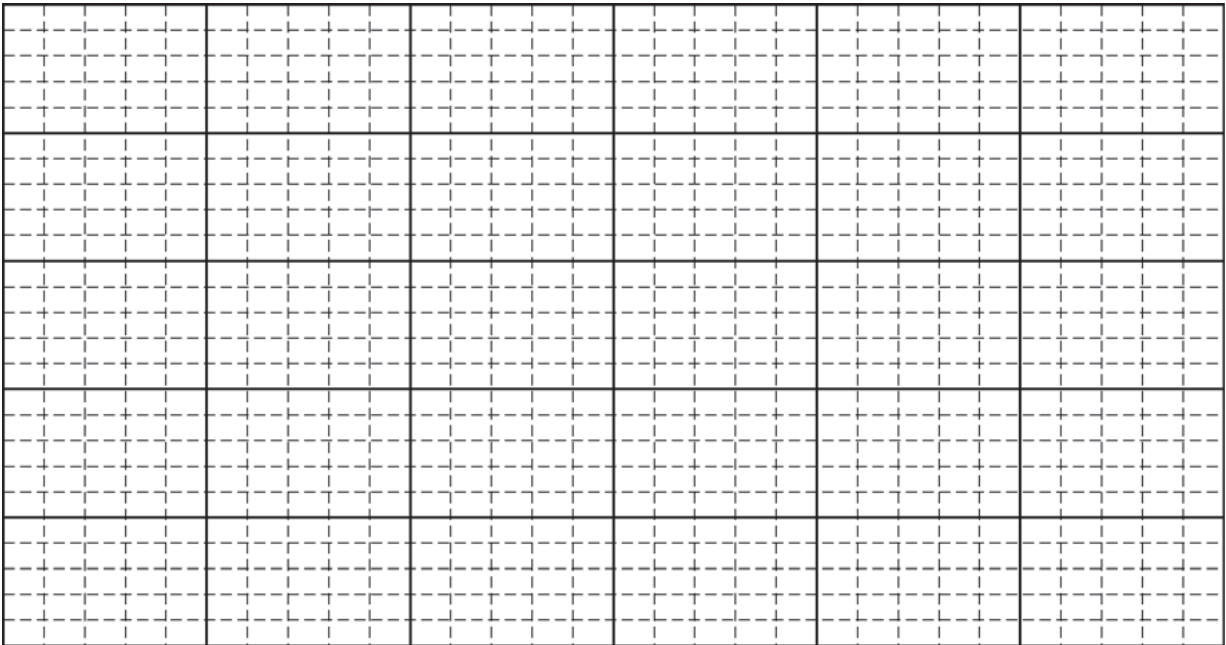
- (c) Indicate below which quantities should be graphed to yield a straight line whose slope could be used to calculate a numerical value for the acceleration due to gravity  $g$ .

Horizontal axis: \_\_\_\_\_

Vertical axis: \_\_\_\_\_

Use the remaining rows in the table above, as needed, to record any quantities that you indicated that are not given. Label each row you use and include units.

- (d) Plot the straight line data points on the grid below. Clearly scale and label all axes, including units as appropriate. Draw a straight line that best represents the data.



- (e)
- Using your straight line, determine an experimental value for  $g$ .
  - Describe two ways in which the effects of air resistance could be reduced.

**STOP**

**END OF EXAM**