

3. A triangular rod of length L and mass M has a nonuniform linear mass density given by the equation $\lambda = \gamma x^2$, where $\gamma = \frac{3M}{L^3}$ and x is the distance from point P at the left end of the rod.
- (a) Using integral calculus, show that the rotational inertia I of the rod about an axis perpendicular to the page and through point P is $\frac{3}{5}ML^2$.
- (b) Determine the horizontal location of the center of mass of the rod relative to point P . Express your answer in terms of L .
- (c) For an axis perpendicular to the page, is the value of the rotational inertia of the rod around point P greater than, less than, or equal to the value of the rotational inertia of the rod around the rod's center of mass?
- _____ Greater than _____ Less than _____ Equal to

Justify your answer.

Use a pencil or pen with black or dark blue ink only. Do NOT write your name. Do NOT write outside the box.

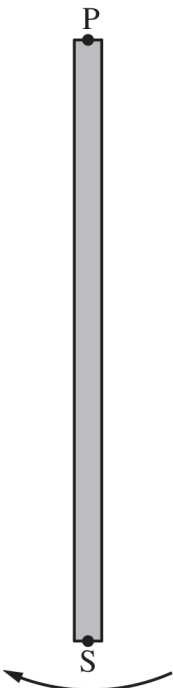
The rod is released from rest in the position shown, and the rod begins to rotate about a horizontal axis perpendicular to the page and through point P .

- (e) As the rod rotates from the horizontal position down through vertical, is the magnitude of the angular acceleration on the rod increasing, decreasing, or not changing?

_____ Increasing _____ Decreasing _____ Not changing

Justify your answer.

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- (f) The mass of the rod is 3.0 kg , and the length of the rod is 1.0 m . Calculate the linear speed v of point S as the rod swings through the vertical position shown.

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STOP

END OF EXAM