

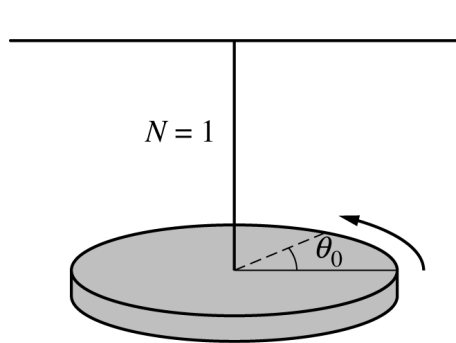


Figure 1

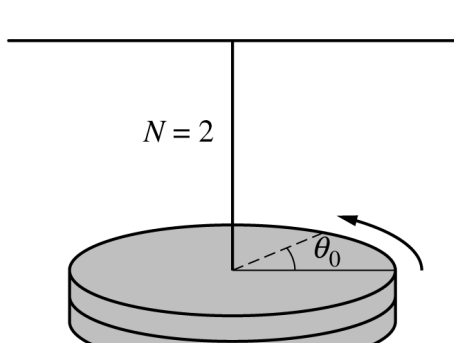


Figure 2

2. A student makes a torsional pendulum by suspending a uniform disk of mass  $M$  and radius  $R$  from a light wire with torsion constant  $\kappa$  that is attached to the center of the disk as shown in Figure 1. The rotational inertia of the disk is given by  $I = \frac{1}{2}MR^2$ . The student conducts an investigation to determine the relationship between the period of oscillation  $T$  of the torsional pendulum and the number  $N$  of identical disks that are suspended from the wire.

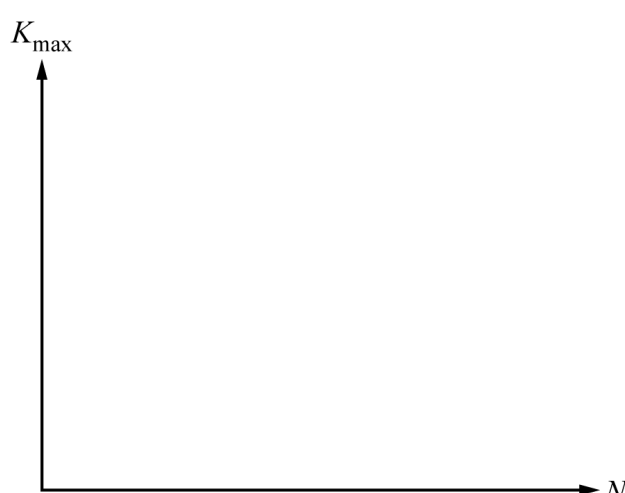
The student starts with a single disk. Holding the disk at a small initial angular displacement  $\theta_0$  from the untwisted position, the student releases the disk from rest and the pendulum oscillates. The student records the period of oscillation for a single disk. An additional identical disk is attached, as shown in Figure 2, and the procedure is repeated for  $N = 2$  disks. This procedure is repeated through  $N = 10$  identical disks. Assume the disks move together as one system.

- (a) Using  $T = 2\pi\sqrt{\frac{I}{\kappa}}$ , derive an expression for  $T$  as a function of  $N$ . Express your answer in terms of  $M$ ,  $R$ ,  $\kappa$ ,  $N$ , and physical constants, as appropriate.

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Continue your response to QUESTION 2 on this page.

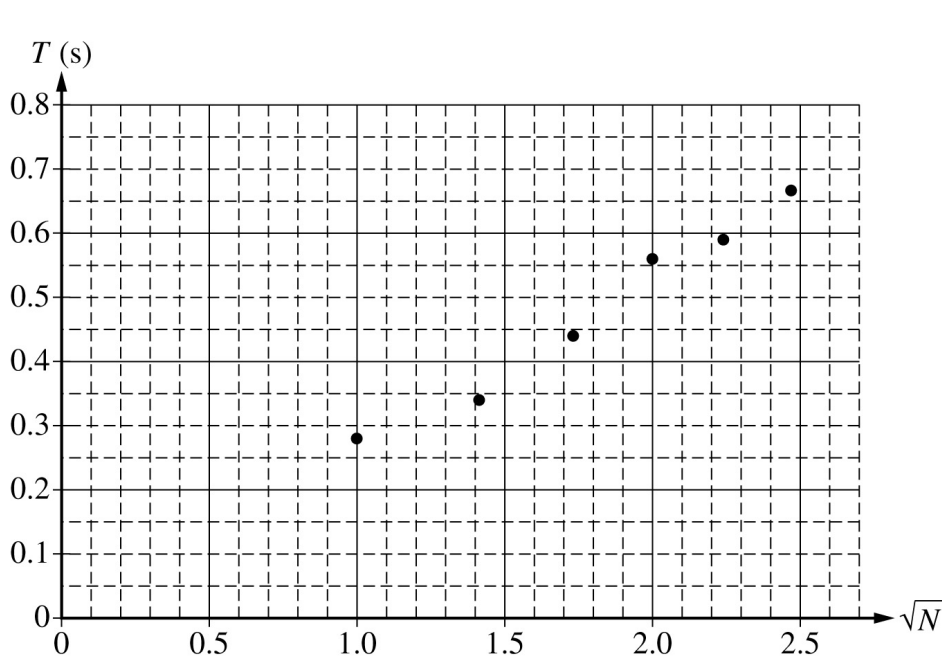
- (b) The potential energy stored in the torsional pendulum when the disks are displaced is  $U = \frac{1}{2}\kappa(\Delta\theta)^2$ . On the following axes, sketch a graph of the maximum kinetic energy  $K_{\max}$  of the torsional pendulum as a function of  $N$  for  $N \geq 1$ .



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- (c) The student plots the data for  $T$  as a function of  $\sqrt{N}$ , as shown.



- Draw the best-fit line for the data.
- The student previously determined that the radius of a disk is  $R = 0.2$  m and found that  $\kappa = 1.6$  N·m. Using the graph, calculate the mass  $M$  of a single disk.
- The student finds that the value given by the manufacturer for the mass of the disk is less than the value determined experimentally in part (c)(ii). Determine a single source of experimental error that could result in the observed difference in the value of  $M$ . Justify your answer.

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- (d) The student repeats the experiment, but now the disks have a density that varies as a function of the radius of the disk according to  $\rho = 0.3r$ .

- i. Would the slope of the best-fit line for this new data be greater than, less than, or the same as the slope of the best-fit line in part (c)(i) ?

\_\_\_ greater than    \_\_\_ less than    \_\_\_ the same as

Justify your answer.

- ii. When  $N = 1$ , the maximum angular speed of the torsional pendulum with a uniform disk is found to be  $\omega_U$ . When  $N = 1$ , the maximum angular speed of the torsional pendulum with a nonuniform disk is  $\omega_{\text{non-U}}$ . Which of the following correctly compares  $\omega_U$  and  $\omega_{\text{non-U}}$  ?

\_\_\_  $\omega_U > \omega_{\text{non-U}}$     \_\_\_  $\omega_U < \omega_{\text{non-U}}$     \_\_\_  $\omega_U = \omega_{\text{non-U}}$

Briefly justify your answer.

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